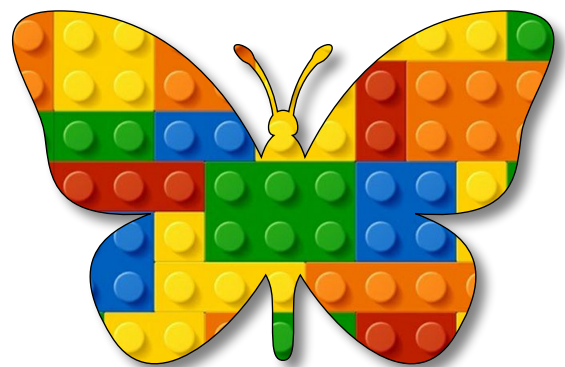


Artificial
Intelligence
Module A
Unit #3
sine wave
regression





Module A Unit #3 sine wave regression

Introduction to sine wave regression

The [index.html](#) file

Sketch A3.1	sine wave sketch
Sketch A3.2	epochs
Sketch A3.3	layers
Sketch A3.4	more hidden layers
Sketch A3.5	more nodes
Sketch A3.6	learning rate
Sketch A3.7	always a bit of trial and error
Sketch A3.8	changing the activation function



Introduction to sine wave regression with ml5.js

In the previous unit we trained a model to predict a straight line, and had a peek at the batch size hyperparameter. This time we are going to make things a bit more challenging. We are going to upgrade from a straight line to a sine wave.

This will give us a chance to look at some more hyperparameters and their impact on the training of the model. We will use them to try to make better predictions of a sine wave.

The hyperparameters we will be looking at will be

- 中 Number of hidden layers
- 中 Number of nodes in each layer
- 中 Activation functions
- 中 Epochs
- 中 Learning Rate



The index.html

Make sure that you have the ml5.js line of code in your index.html file

```
<!DOCTYPE html>
<html lang="en">
  <head>
    <script src="https://cdnjs.cloudflare.com/ajax/libs/p5.js/1.11.0/p5.js"></script>
    <script src="https://cdnjs.cloudflare.com/ajax/libs/p5.js/1.11.0/addons/p5.sound.min.js"></script>
    <script src="https://unpkg.com/ml5@1/dist/ml5.min.js"></script>
    <link rel="stylesheet" type="text/css" href="style.css">
    <meta charset="utf-8" />

  </head>
  <body>
    <main>
    </main>
    <script src="sketch.js"></script>
  </body>
</html>
```



Sketch A3.1 sine wave sketch

We are starting with the sketch from linear regression. Then we'll modify the data because instead of a line we want a sine wave. In p5.js the default angle units are radians, but we are going to work in degrees which is a little more intuitive. To make this change, we use the function `angleMode()` in `setup()`. Everything else in the sketch remains the same.

```
let nn
let counter = 0
let data
const number = 30
const spread = 30
const options = {
  task: 'regression',
  debug: true
}

function setup()
{
  createCanvas(400, 400)
  angleMode(DEGREES)
  ml5.setBackend("webgl")
  nn = ml5.neuralNetwork(options)
  trainingData()
  nn.normalizeData()
  const trainingOptions = {
    batchSize: 512
  }
  nn.train(trainingOptions, finishedTraining)
}

function trainingData()
```

```

{
  background(220)
  for (let i = 0; i < width; i += 10)
  {
    for (let j = 0; j < number; j++)
    {
      data = [i + floor(random(-spread, spread)), 200 + (50 *
sin(i) + floor(random(-spread, spread)))]
      fill(0, 0, 255)
      noStroke()
      circle(data[0], data[1], 5)
      nn.addData([data[0]], [data[1]])
    }
  }
}

function finishedTraining()
{
  if (counter < 400)
  {
    nn.predict([counter], gotResults)
  }
}

function gotResults(results)
{
  let prediction = results[0]
  let x = counter
  let y = prediction.value
  stroke(255, 0, 0)
  strokeWeight(5)
  point(x, y)
  counter++
}

```

```
finishedTraining()  
}
```



Notes

For every **x** input we get the sine of that input as our **y** output. We multiply by **50** to increase the amplitude (otherwise a very flat sine wave) and move it by **200** pixels so we have it in the centre of the canvas, plus the usual variance, **random(spread)**. The results aren't as bad as you might expect as it uses default settings for most of the hyperparameters except for the batch size.



Code Explanation

<code>angleMode(DEGREES)</code>	This changes the default to degrees (notice all capitals)
<code>sin(i)</code>	Returns the sine of i

Figure A3.1a loss chart

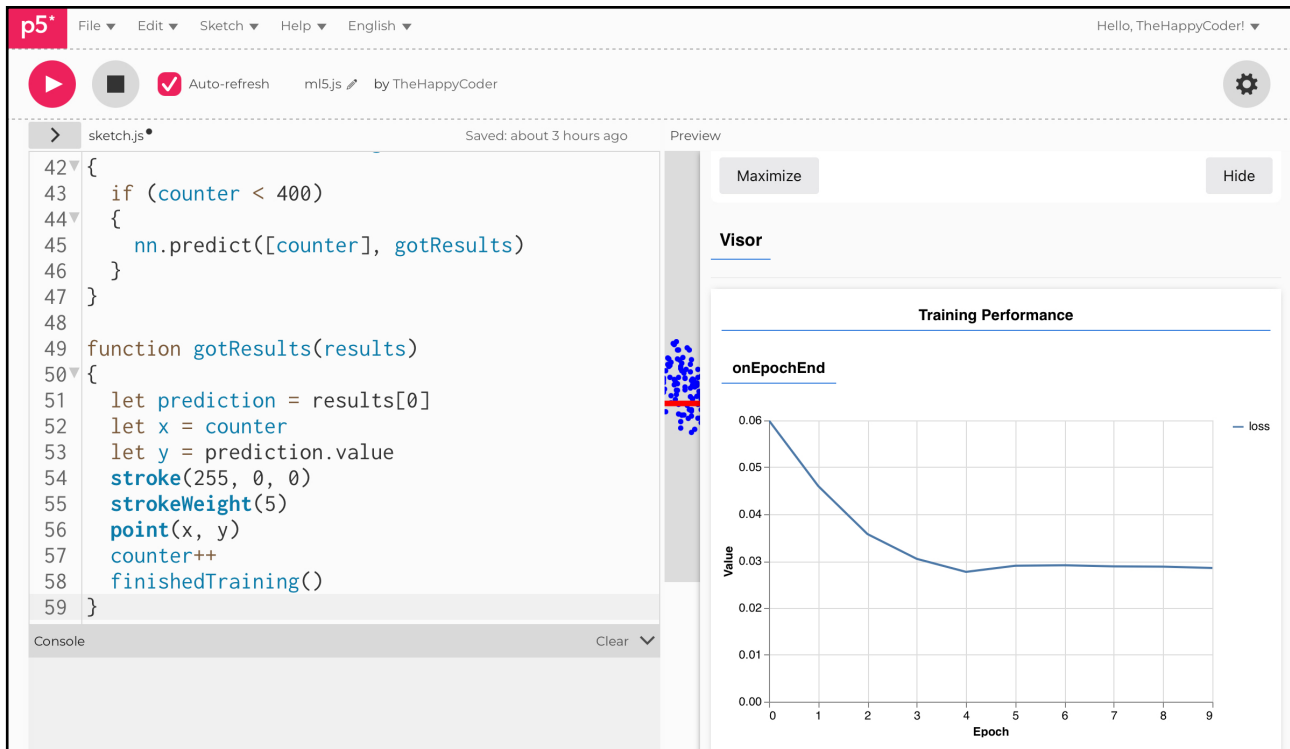


Figure A3.1b predicted results





Sketch A3.2 epochs

Our first **hyperparameter** change will be the number of **epochs**. Each epoch is one complete dataset. Currently we are only running **10 epochs** and it looks as if the loss might be still going down after that. Let's extend it to **100 epochs** and see where it levels off (or stops learning). We can introduce this **hyperparameter** into the training options just like we did with the batch sizes.

! You will need to put a **comma (,)** after the **512**.

```
let nn
let counter = 0
let data
const number = 30
const spread = 30
const options = {
  task: 'regression',
  debug: true
}

function setup()
{
  createCanvas(400, 400)
  angleMode(DEGREES)
  ml5.setBackend("webgl")
  nn = ml5.neuralNetwork(options)
  trainingData()
  nn.normalizeData()
  const trainingOptions = {
    batchSize: 512,
    epochs: 100
  }
  nn.train(trainingOptions, finishedTraining)
```

```

}

function trainingData()
{
  background(220)
  for (let i = 0; i < width; i += 10)
  {
    for (let j = 0; j < number; j++)
    {
      data = [i + floor(random(-spread, spread)), 200 + (50 *
sin(i) + floor(random(-spread, spread)))]
      fill(0, 0, 255)
      noStroke()
      circle(data[0], data[1], 5)
      nn.addData([data[0]], [data[1]])
    }
  }
}

function finishedTraining()
{
  if (counter < 400)
  {
    nn.predict([counter], gotResults)
  }
}

function gotResults(results)
{
  let prediction = results[0]
  let x = counter
  let y = prediction.value
  stroke(255, 0, 0)

```

```
strokeWeight(5)
point(x, y)
counter++
finishedTraining()
}
```



Notes

The changes were not a great improvement. You may get slightly different results depending on how the weights are initialised in the model but it seems to level out after around 10 epochs.



Challenge

Try again with different epoch settings.



Code Explanation

epochs:100	Defines how many epochs if not using the default value
------------	--

Figure A3.2

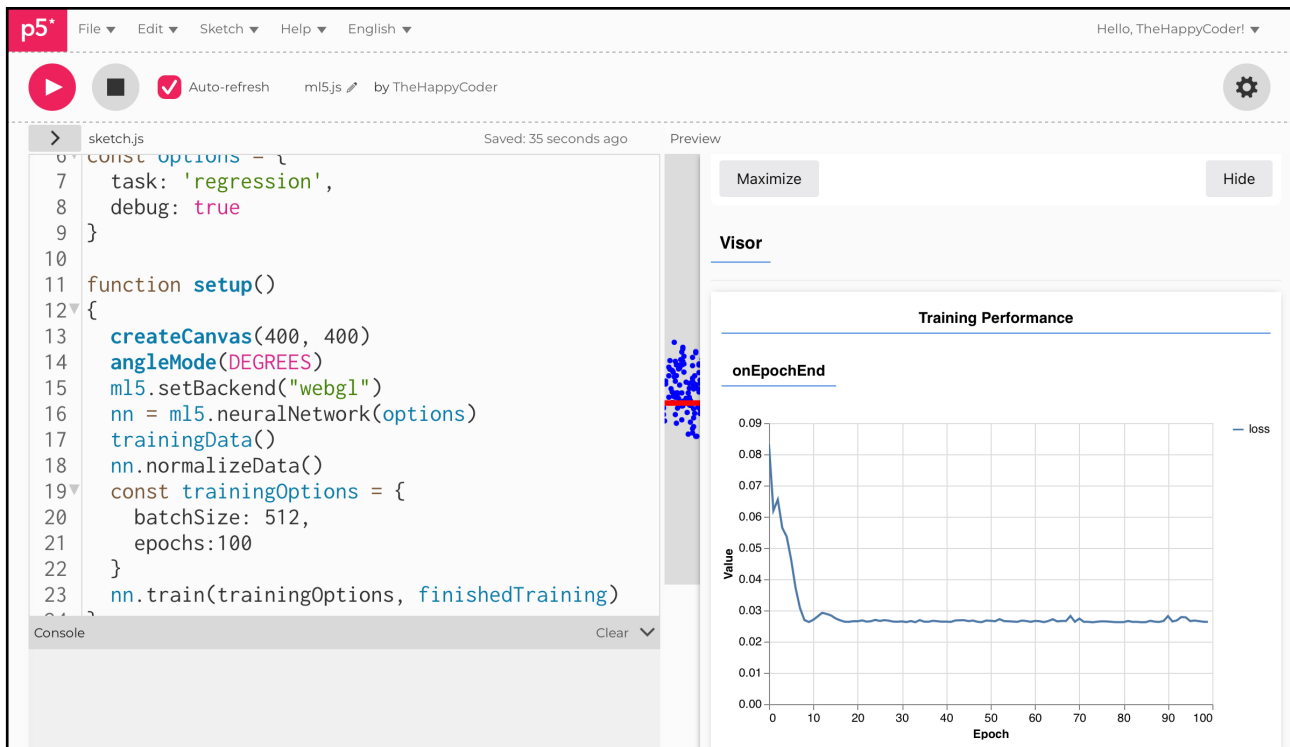
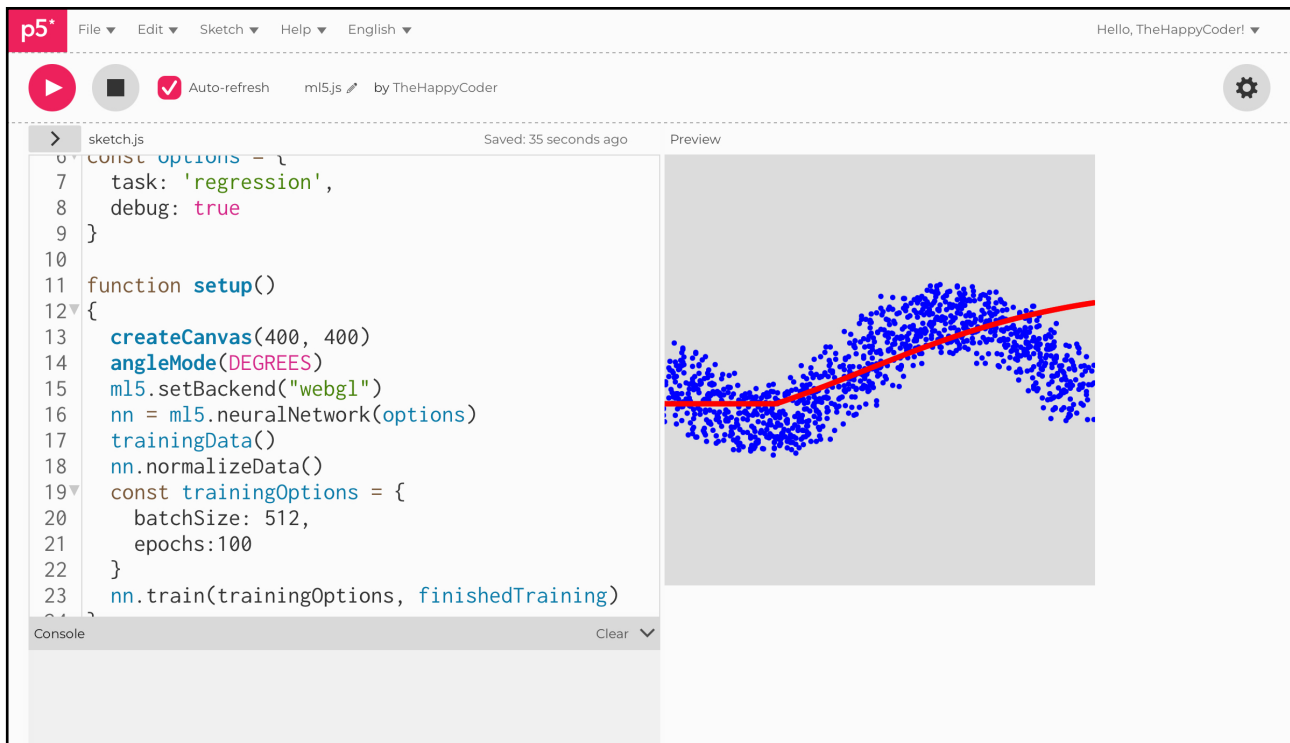


Figure A3.2





Sketch A3.3 layers

We can add more layers, more accurately we can add more hidden layers. In those layers we can specify the number of nodes and the activation function we want to use. The default settings are shown below:



Input Layer

One input node



Output Layer

One output node



Hidden Layer

By default we have one hidden layer with 16 nodes



Dense

Means all the nodes in one layer are fully connected to the node in the previous layer.



Activation Functions

In the hidden layer they are the **ReLU** function and for the output layer it is the **sigmoid** function

```
let nn
let counter = 0
let data
const number = 30
const spread = 30
const options = {
  task: 'regression',
  layers: [
    {
      type: 'dense',
      units: 16,
      activation: 'relu'
    }
  ]
}
```

```

    },
    {
      type: 'dense',
      activation: 'sigmoid'
    }
  ],
  debug: true
}

function setup()
{
  createCanvas(400, 400)
  angleMode(DEGREES)
  ml5.setBackend("webgl")
  nn = ml5.neuralNetwork(options)
  trainingData()
  nn.normalizeData()
  const trainingOptions = {
    batchSize: 512,
    epochs: 100
  }
  nn.train(trainingOptions, finishedTraining)
}

function trainingData()
{
  background(220)
  for (let i = 0; i < width; i += 10)
  {
    for (let j = 0; j < number; j++)
    {
      data = [i + floor(random(-spread, spread)), 200 + (50 *
sin(i) + floor(random(-spread, spread)))]
    }
  }
}

```

```

        fill(0, 0, 255)
        noStroke()
        circle(data[0], data[1], 5)
        nn.addData([data[0]], [data[1]])
    }
}

function finishedTraining()
{
    if (counter < 400)
    {
        nn.predict([counter], gotResults)
    }
}

function finishedTraining()
{
    if (counter < 400)
    {
        nn.predict([counter], gotResults)
    }
}

function gotResults(results)
{
    let prediction = results[0]
    let x = counter
    let y = prediction.value
    stroke(255, 0, 0)
    strokeWeight(5)
    point(x, y)
    counter++
}

```

```
finishedTraining()  
}
```



Notes

As you can see it has made no difference, which is really as expected. If you get a better (or worse) result just remember that it is starting each time with different (random) weights as well as random data.



Challenge

You might want to start changing the number of nodes in the hidden layer



Code Explanation

layers: [...]	Adding layers in the training option
type: 'dense'	Fully connected nodes between each layer
units: 16	16 nodes (neurons) in the hidden layer
activation: 'relu'	Hidden layer activation function
activation: 'sigmoid'	Output layer activation function

Figure A3.3a

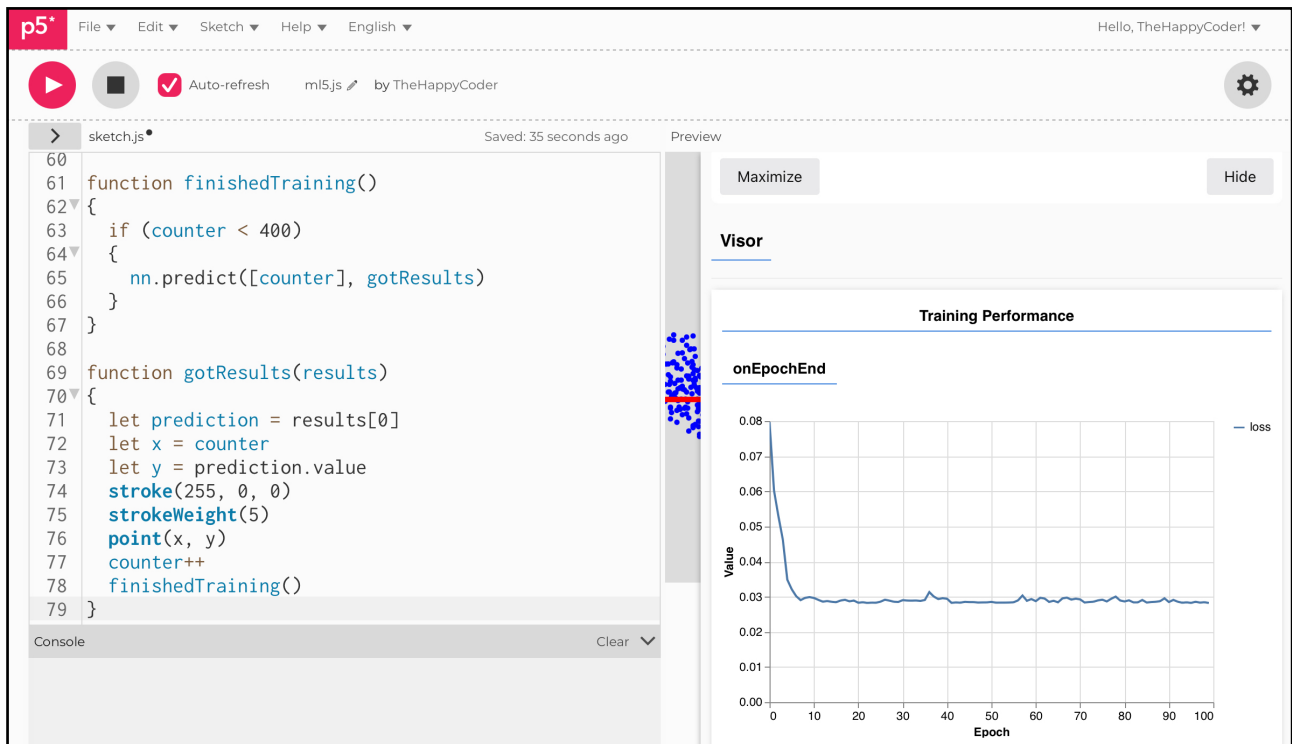
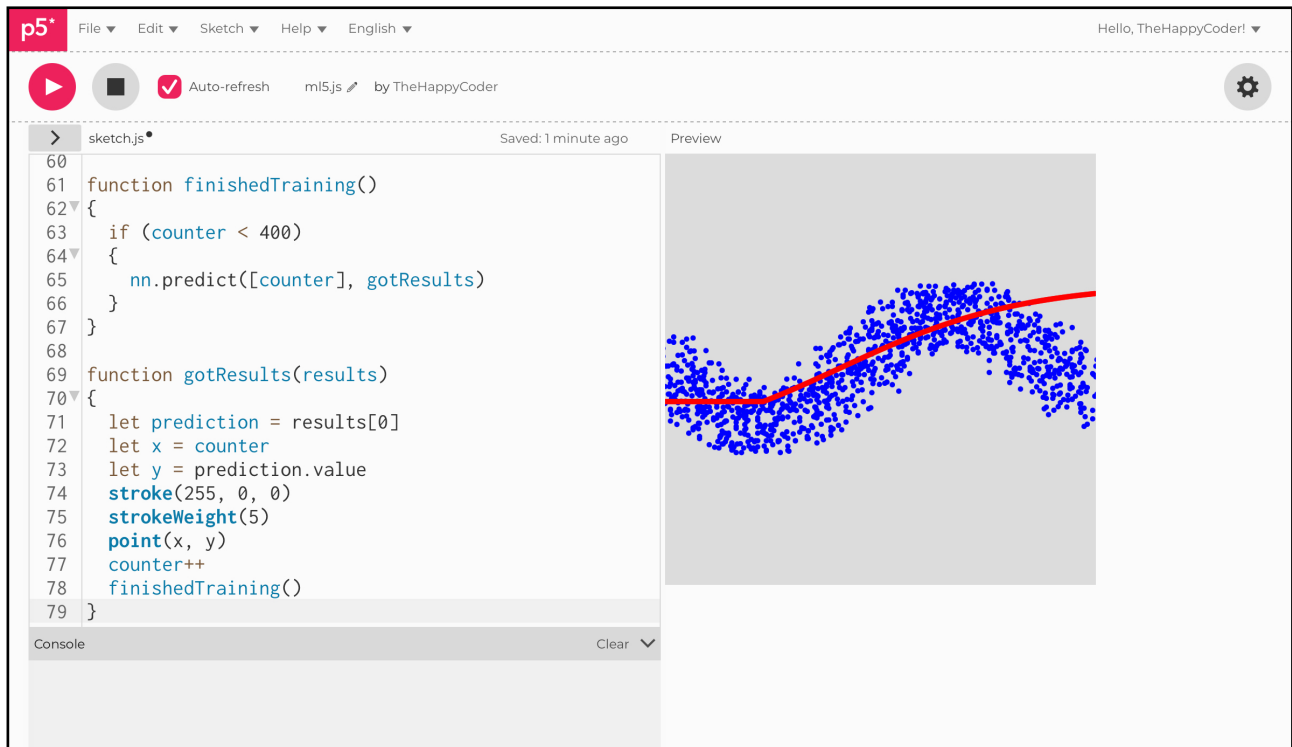


Figure A3.3b





Sketch A3.4 more hidden layers

Added two more identical hidden layers

```
let nn
let counter = 0
let data
const number = 30
const spread = 30
const options = {
  task: 'regression',
  layers: [
    {
      type: 'dense',
      units: 16,
      activation: 'relu'
    },
    {
      type: 'dense',
      units: 16,
      activation: 'relu'
    },
    {
      type: 'dense',
      units: 16,
      activation: 'relu'
    },
    {
      type: 'dense',
      activation: 'sigmoid'
    }
  ],
  debug: true
}
```

```

}

function setup()
{
  createCanvas(400, 400)
  angleMode(DEGREES)
  ml5.setBackend("webgl")
  nn = ml5.neuralNetwork(options)
  trainingData()
  nn.normalizeData()
  const trainingOptions = {
    batchSize: 512,
    epochs:100
  }
  nn.train(trainingOptions, finishedTraining)
}

function trainingData()
{
  background(220)
  for (let i = 0; i < width; i += 10)
  {
    for (let j = 0; j < number; j++)
    {
      data = [i + floor(random(-spread, spread)), 200 + (50 *
sin(i) + floor(random(-spread, spread)))]
      fill(0, 0, 255)
      noStroke()
      circle(data[0], data[1], 5)
      nn.addData([data[0]], [data[1]])
    }
  }
}

```

```
function finishedTraining()
{
  if (counter < 400)
  {
    nn.predict([counter], gotResults)
  }
}

function gotResults(results)
{
  let prediction = results[0]
  let x = counter
  let y = prediction.value
  stroke(255, 0, 0)
  strokeWeight(5)
  point(x, y)
  counter++
  finishedTraining()
}
```



Notes

You can see in my example the beginnings of a sine wave but far from what we might want.

Figure A3.4a

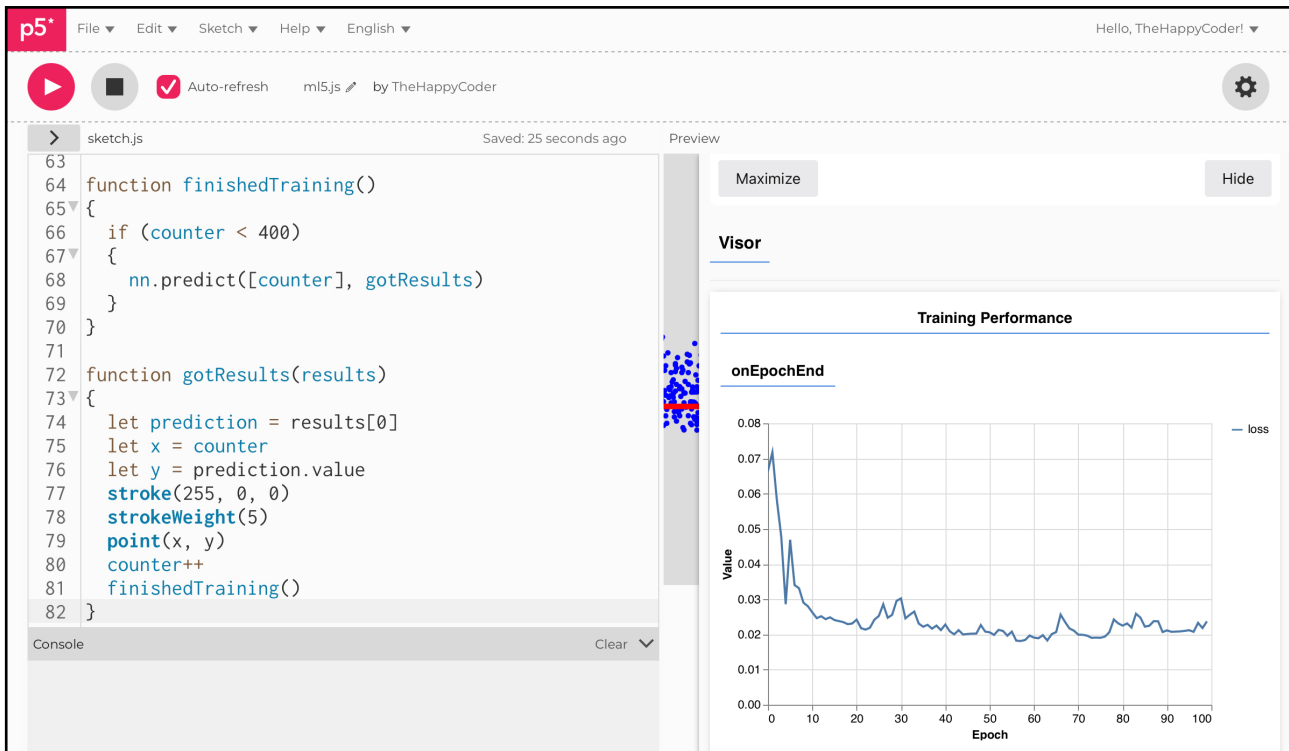
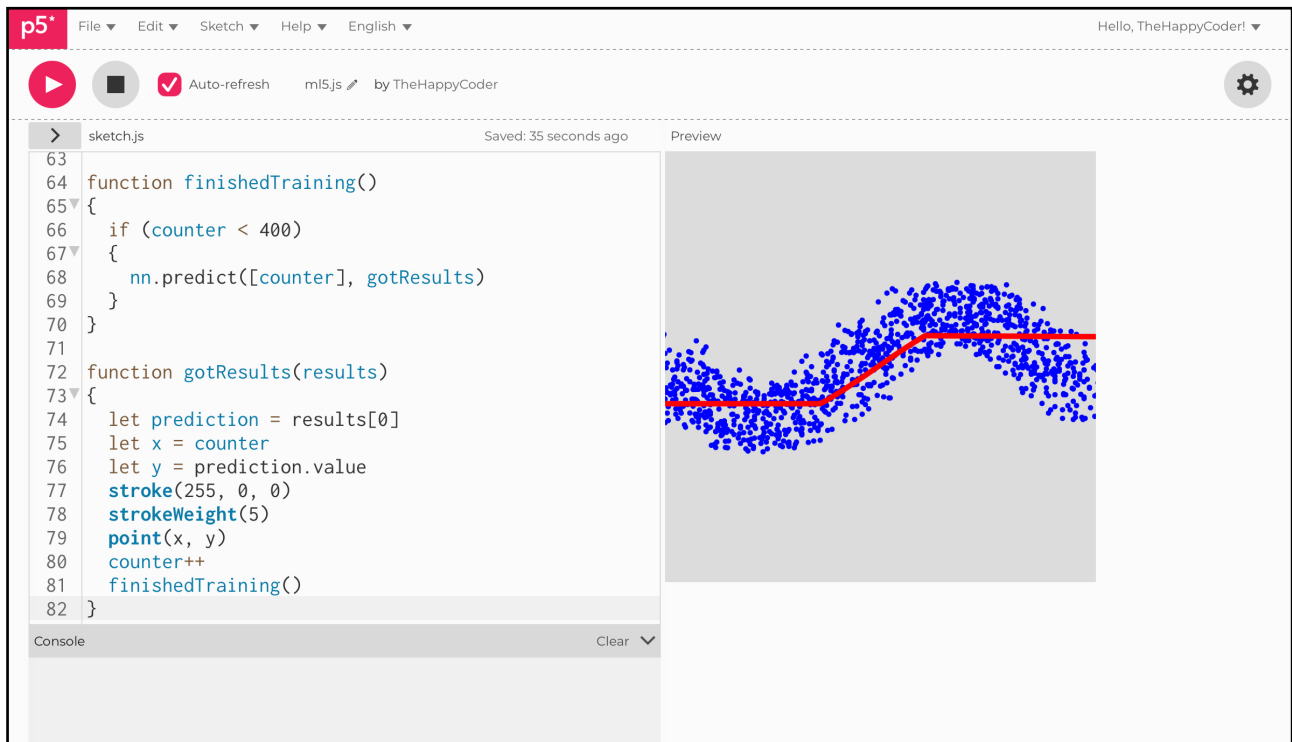


Figure A3.4b





Sketch A3.5 more nodes

Increasing the number of nodes, they don't have to be equal for each hidden layer, it is worth trying mixing it up a bit to see what happens.

```
let nn
let counter = 0
let data
const number = 30
const spread = 30
const options = {
  task: 'regression',
  layers: [
    {
      type: 'dense',
      units: 64,
      activation: 'relu'
    },
    {
      type: 'dense',
      units: 64,
      activation: 'relu'
    },
    {
      type: 'dense',
      units: 64,
      activation: 'relu'
    },
    {
      type: 'dense',
      activation: 'sigmoid'
    }
  ],
}
```

```

    debug: true
  }

function setup()
{
  createCanvas(400, 400)
  angleMode(DEGREES)
  ml5.setBackend("webgl")
  nn = ml5.neuralNetwork(options)
  trainingData()
  nn.normalizeData()
  const trainingOptions = {
    batchSize: 512,
    epochs:100
  }
  nn.train(trainingOptions, finishedTraining)
}

function trainingData()
{
  background(220)
  for (let i = 0; i < width; i += 10)
  {
    for (let j = 0; j < number; j++)
    {
      data = [i + floor(random(-spread, spread)), 200 + (50 *
sin(i) + floor(random(-spread, spread)))]
      fill(0, 0, 255)
      noStroke()
      circle(data[0], data[1], 5)
      nn.addData([data[0]], [data[1]])
    }
  }
}

```

```
}

function finishedTraining()
{
  if (counter < 400)
  {
    nn.predict([counter], gotResults)
  }
}

function gotResults(results)
{
  let prediction = results[0]
  let x = counter
  let y = prediction.value
  stroke(255, 0, 0)
  strokeWeight(5)
  point(x, y)
  counter++
  finishedTraining()
}
```



Notes

You can see the pattern emerging but still less than satisfactory.



Challenge

Think about more/fewer nodes, more/fewer layers

Figure A3.5a

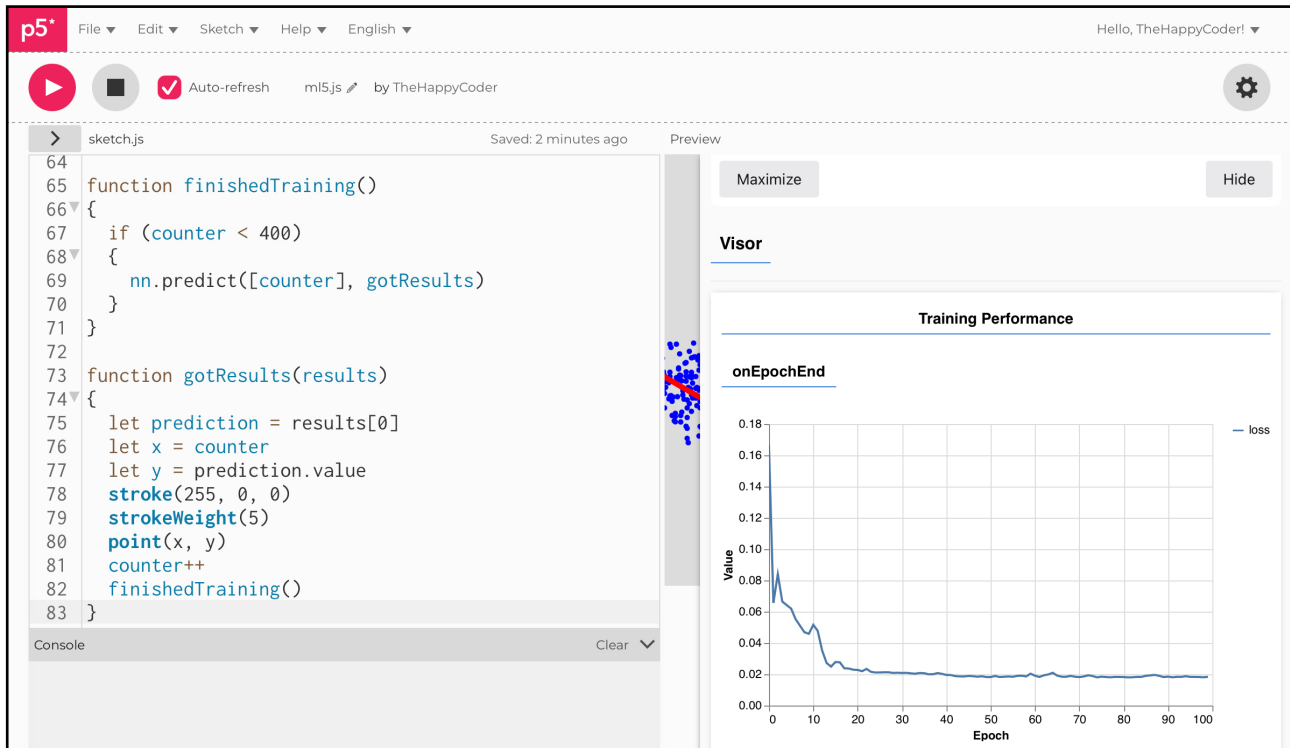
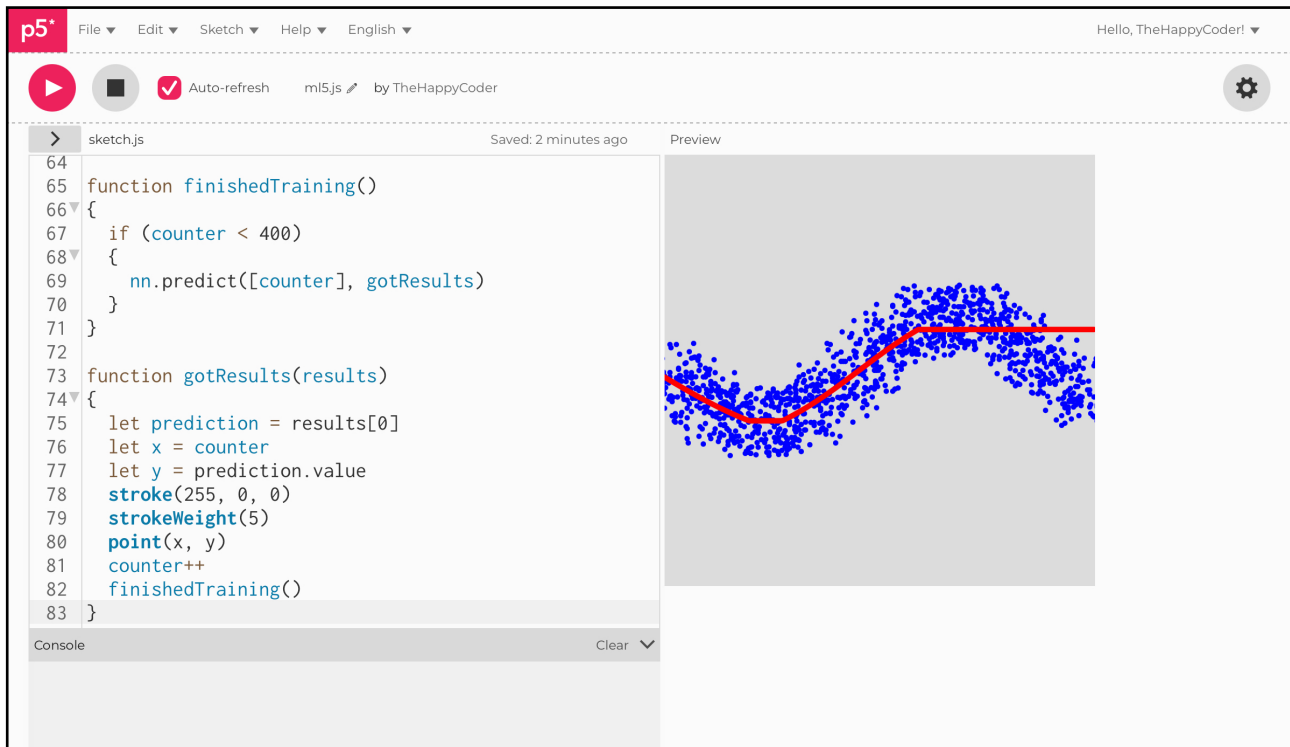


Figure A3.5b





Sketch A3.6 learning rate

Another **hyperparameter** we can change is the **learning rate**. The **learningRate** are the size of steps the algorithm takes to find the lowest point in the calculations. If the steps are too big they can miss the global minimum, too small and it can never find the minimum and gets stuck on a local minimum. We are keeping the number of layers and nodes the same as the previous sketch.

```
let nn
let counter = 0
let data
const number = 30
const spread = 30
const options = {
  task: 'regression',
  learningRate: 0.1,
  layers: [
    {
      type: 'dense',
      units: 64,
      activation: 'relu'
    },
    {
      type: 'dense',
      units: 64,
      activation: 'relu'
    },
    {
      type: 'dense',
      units: 64,
      activation: 'relu'
    },
    {
```

```

        type: 'dense',
        activation: 'sigmoid'
    }
],
debug: true
}

function setup()
{
    createCanvas(400, 400)
    angleMode(DEGREES)
    ml5.setBackend("webgl")
    nn = ml5.neuralNetwork(options)
    trainingData()
    nn.normalizeData()
    const trainingOptions = {
        batchSize: 512,
        epochs:100
    }
    nn.train(trainingOptions, finishedTraining)
}

function trainingData()
{
    background(220)
    for (let i = 0; i < width; i += 10)
    {
        for (let j = 0; j < number; j++)
        {
            data = [i + floor(random(-spread, spread)), 200 + (50 *
sin(i) + floor(random(-spread, spread)))]
            fill(0, 0, 255)
            noStroke()

```

```

        circle(data[0], data[1], 5)
        nn.addData([data[0]], [data[1]])
    }
}

function finishedTraining()
{
    if (counter < 400)
    {
        nn.predict([counter], gotResults)
    }
}

function gotResults(results)
{
    let prediction = results[0]
    let x = counter
    let y = prediction.value
    stroke(255, 0, 0)
    strokeWeight(5)
    point(x, y)
    counter++
    finishedTraining()
}

```



Notes

Not a significant difference but the loss function is very jumpy



Challenge

I could fiddle with these values endlessly and that is why Machine Learning is an art as much as a science. I will let you play around perhaps trying learning rates of **1** or **0.001**, more nodes but fewer hidden layers.

Code Explanation

```
learningRate: 0.1
```

We can specify the learning rate, the steps (or jumps) in the training process

Figure A3.6a

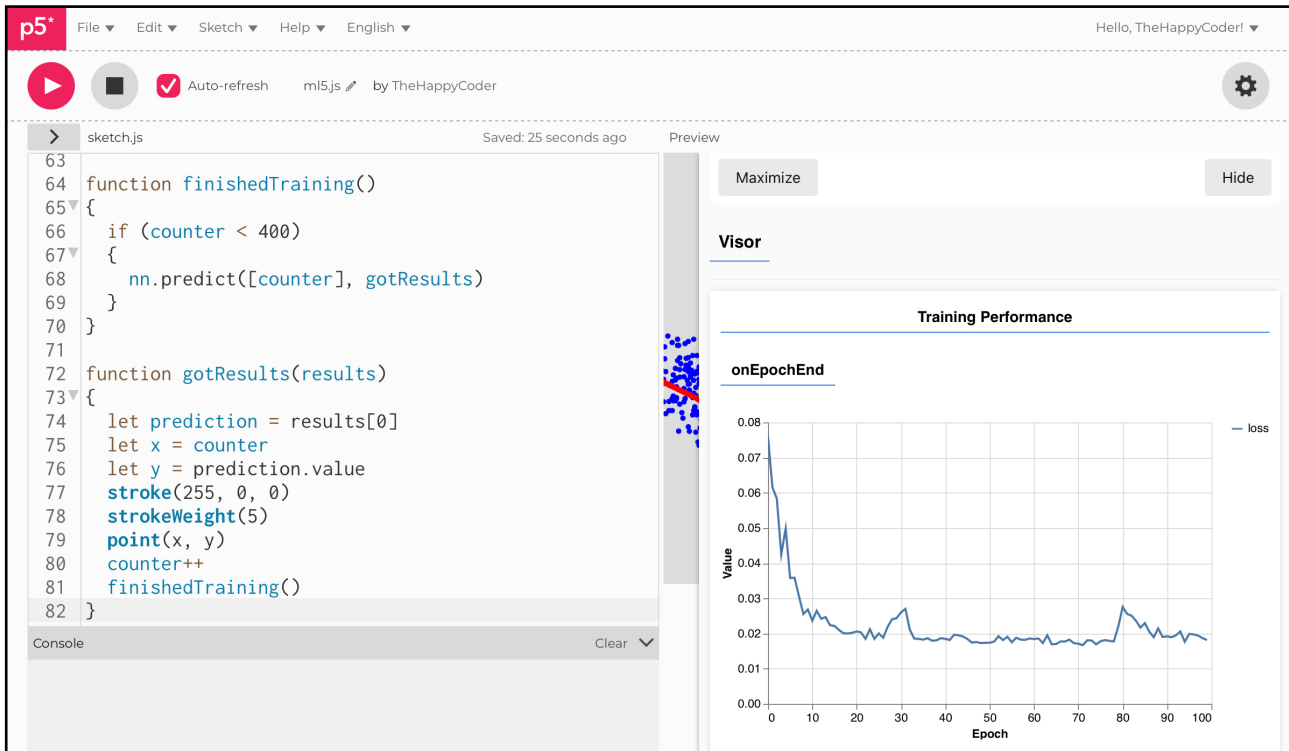
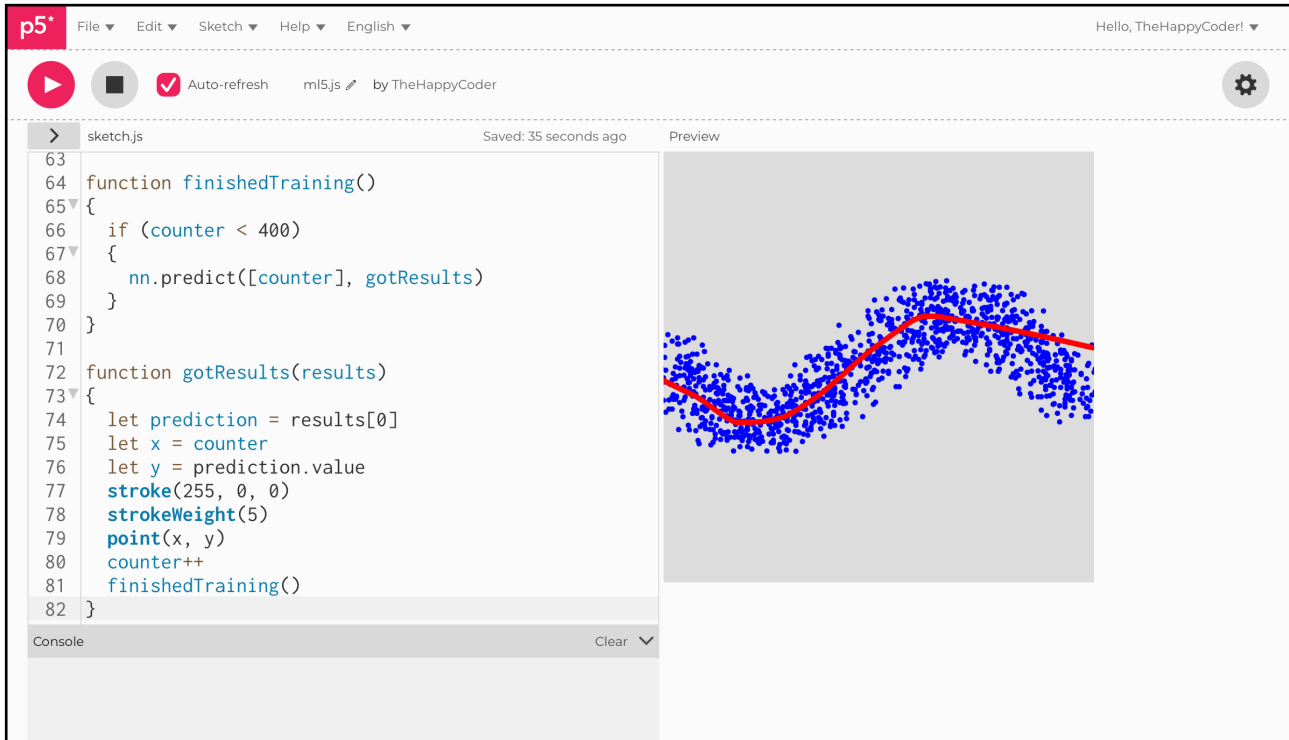


Figure A3.6b





Sketch A3.7 always a bit of trial and error

I have increased the number of nodes but reduced the number of layers, as well as reducing the learning rate to **0.01**.

```
let nn
let counter = 0
let data
const number = 30
const spread = 30
const options = {
  task: 'regression',
  learningRate: 0.01,
  layers: [
    {
      type: 'dense',
      units: 256,
      activation: 'relu'
    },
    {
      type: 'dense',
      units: 256,
      activation: 'relu'
    },
    {
      type: 'dense',
      activation: 'sigmoid'
    }
  ],
  debug: true
}

function setup()
```

```

{
  createCanvas(400, 400)
  angleMode(DEGREES)
  ml5.setBackend("webgl")
  nn = ml5.neuralNetwork(options)
  trainingData()
  nn.normalizeData()
  const trainingOptions = {
    batchSize: 512,
    epochs:100
  }
  nn.train(trainingOptions, finishedTraining)
}

function trainingData()
{
  background(220)
  for (let i = 0; i < width; i += 10)
  {
    for (let j = 0; j < number; j++)
    {
      data = [i + floor(random(-spread, spread)), 200 + (50 *
sin(i) + floor(random(-spread, spread)))]
      fill(0, 0, 255)
      noStroke()
      circle(data[0], data[1], 5)
      nn.addData([data[0]], [data[1]])
    }
  }
}

function finishedTraining()
{

```

```
    if (counter < 400)
    {
        nn.predict([counter], gotResults)
    }
}

function gotResults(results)
{
    let prediction = results[0]
    let x = counter
    let y = prediction.value
    stroke(255, 0, 0)
    strokeWeight(5)
    point(x, y)
    counter++
    finishedTraining()
}
```



Notes

Starting to see some improvements. Bear in mind however that every time you run the code we are using different data (not saved or uploaded) but this is for ease of use and demonstration purposes.



Challenge

Play around with the number of **nodes** and **learning rate**, consider saving the data in the first place and then experimenting with the hyperparameters.

Figure A3.7a

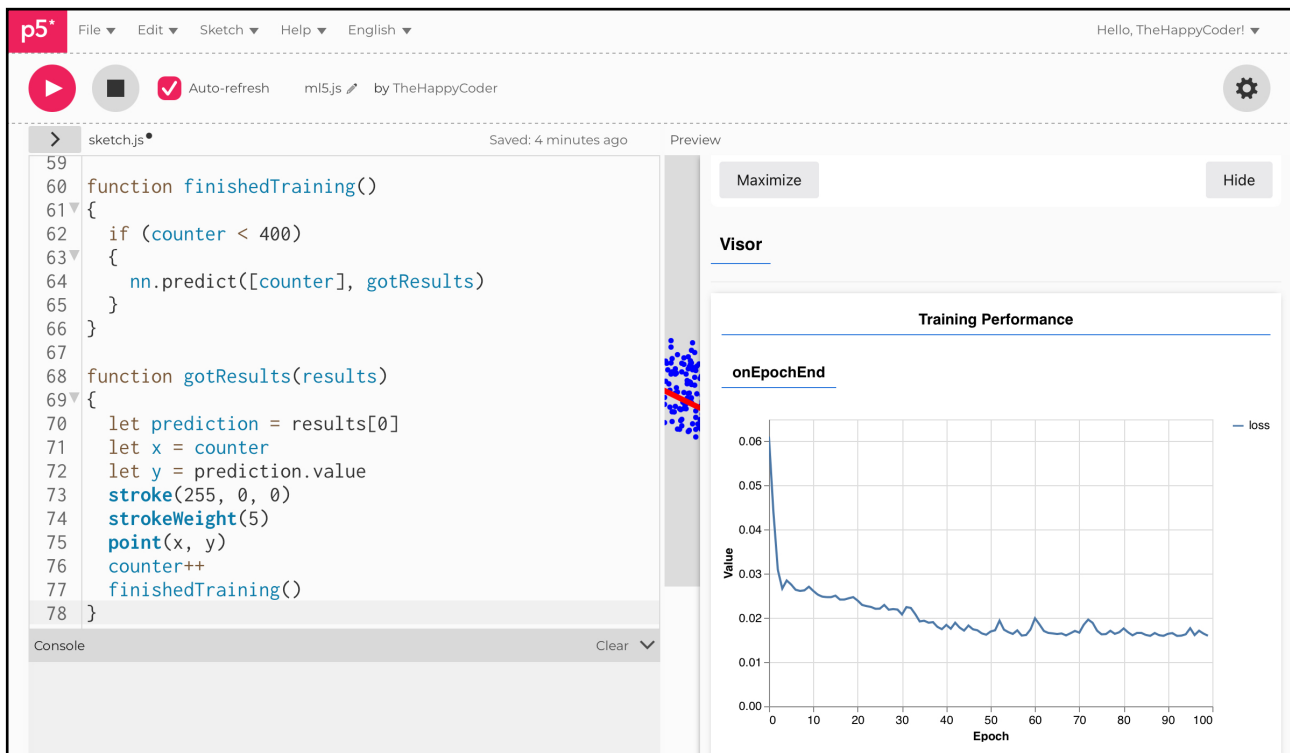
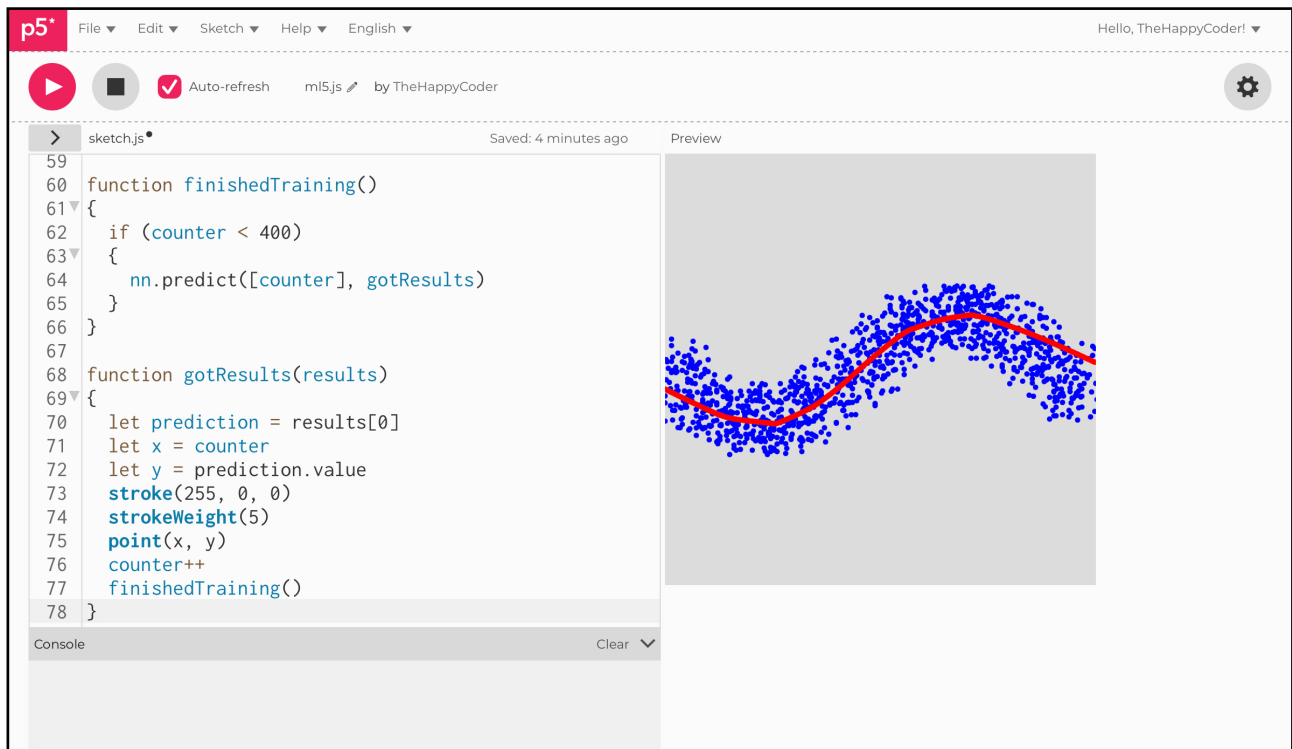


Figure A3.7b





Activation functions

The final hyperparameter we are going to look at is the activation functions. The default for a regression task is hidden layer: **ReLU** and output layer: **Sigmoid**

Just to save on space I will not change any other lines of code except the options layers, so the rest of the code remains the same and is omitted for brevity.



Sketch A3.8 changing the activation function

Using the same **hyperparameters**, we will switch the **ReLU** to **sigmoid**.

```
let nn
let counter = 0
let data
const number = 30
const spread = 30
const options = {
  task: 'regression',
  learningRate: 0.01,
  layers: [
    {
      type: 'dense',
      units: 256,
      activation: 'sigmoid'
    },
    {
      type: 'dense',
      units: 256,
      activation: 'sigmoid'
    },
    {
      type: 'dense',
      activation: 'sigmoid'
    }
  ],
  debug: true
}

function setup()
{
```

```

    createCanvas(400, 400)
    angleMode(DEGREES)
    ml5.setBackend("webgl")
    nn = ml5.neuralNetwork(options)
    trainingData()
    nn.normalizeData()
    const trainingOptions = {
      batchSize: 512,
      epochs:100
    }
    nn.train(trainingOptions, finishedTraining)
    console.log()
  }

function trainingData()
{
  background(220)
  for (let i = 0; i < width; i += 10)
  {
    for (let j = 0; j < number; j++)
    {
      data = [i + floor(random(-spread, spread)), 200 + (50 *
sin(i) + floor(random(-spread, spread)))]
      fill(0, 0, 255)
      noStroke()
      circle(data[0], data[1], 5)
      nn.addData([data[0]], [data[1]])
    }
  }
}

function finishedTraining()
{

```

```
    if (counter < 400)
    {
        nn.predict([counter], gotResults)
    }
}

function gotResults(results)
{
    let prediction = results[0]
    let x = counter
    let y = prediction.value
    stroke(255, 0, 0)
    strokeWeight(5)
    point(x, y)
    counter++
    finishedTraining()
}
```



Notes

Oh, dear! **ReLU** gives consistently better results. It is more efficient and is the industry standard. You could see if you can get better results with fewer/more layers and nodes, I will leave that with you to experiment.



Challenge

Use **tanh** instead of **sigmoid**

Figure A3.8a

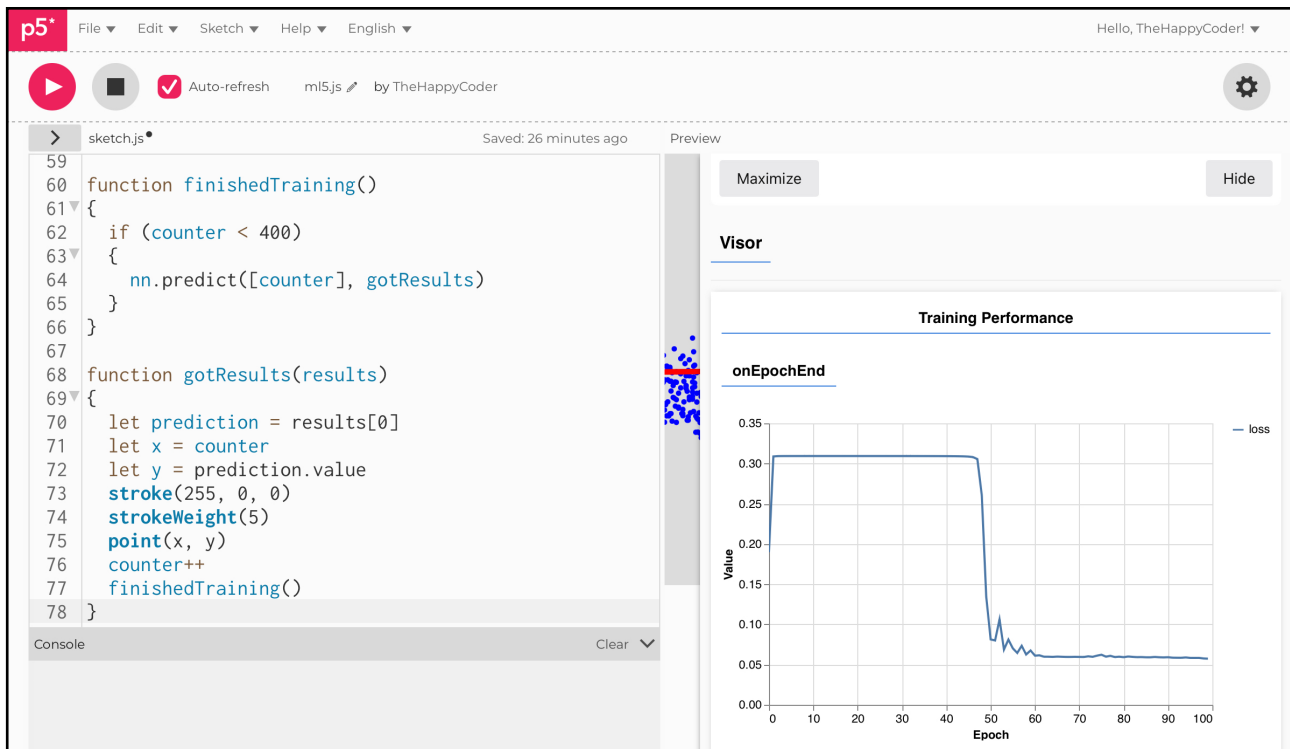
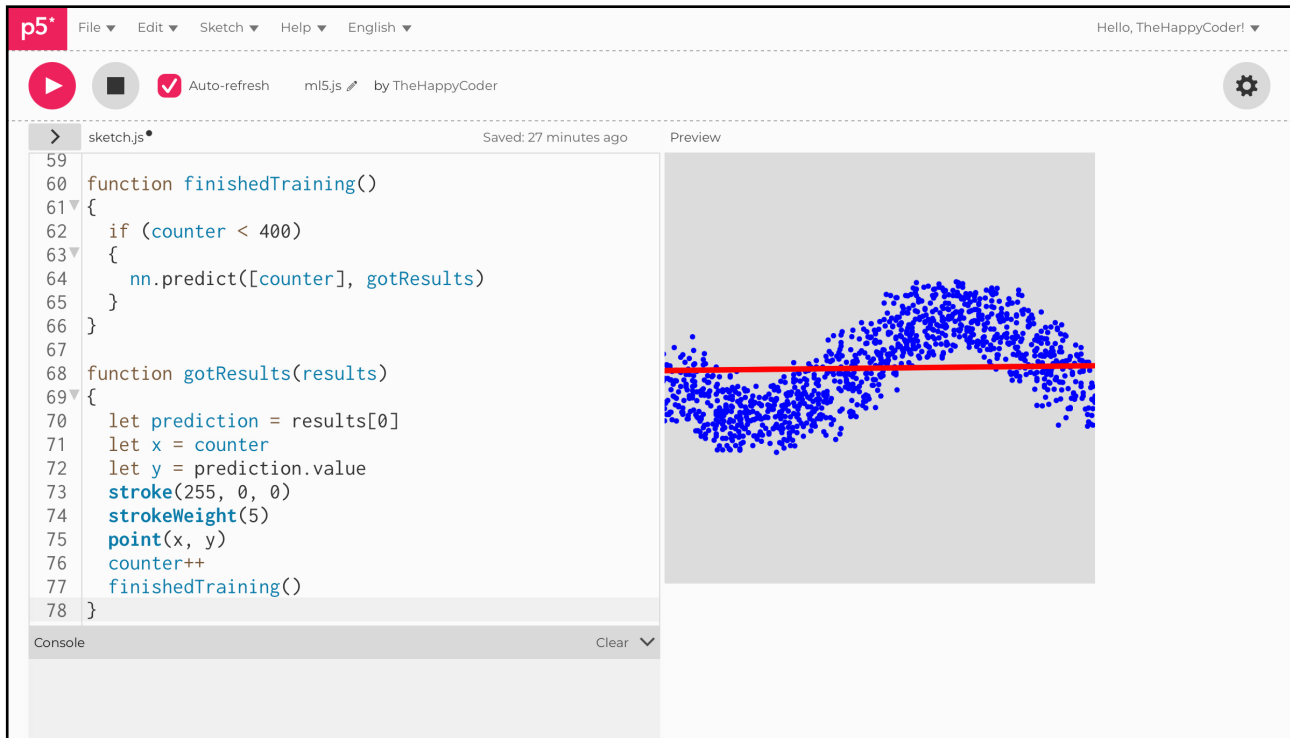


Figure A3.8b





Final challenges

We have looked at the following **hyperparameters**:

- ☑ batch size
- ☑ epochs
- ☑ hidden layers
- ☑ nodes
- ☑ activation functions
- ☑ learning rate

I would strongly recommend playing with all of these and seeing how they impact on the model's learning. Remember that you will never get a perfect result. Also try drawing the sine wave as a single line rather than a scatter graph approach as we did with the linear regression.



Summary

You will probably start to realise that throwing more nodes and hidden layers at the dataset doesn't necessarily improve the outcome, you may also realise having a smaller learning rate, smaller batch size may give you some slightly improved outcome but you may have to wait a considerably longer time. Remember in the real world time and energy is money.